

# 3 Algebra with Variables on Both Sides

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Math 9 Ch 6

Name: \_\_\_\_\_

Level 3: Algebra with Variables on BOTH Sides of the Equation (6.1-6.2) Page 1 of 2

**Learning Outcome 6A:** I can solve algebra equations with variables on **both** sides.

If the equation contains variables on both sides of the equation, simply move one term with the variable to the other side. Think "zero pairs".

**Example 1:** Solve:  $2x + 5 = 3x - 7$ .

Using Algebra Tiles (pictures)

Variable on **right** side.

$$\begin{array}{r}
 2x + 5 = 3x - 7 \\
 -2x \quad -2x \\
 \hline
 5 = x - 7 \\
 +7 \quad +7 \\
 \hline
 12 = x \\
 \boxed{x = 12}
 \end{array}$$

Variable on **left** side.

$$\begin{array}{r}
 2x + 5 = 3x - 7 \\
 -3x \quad -3x \\
 \hline
 -x + 5 = -7 \\
 -5 \quad -5 \\
 \hline
 -x = -12 \\
 \frac{-x}{-1} = \frac{-12}{-1} \\
 \boxed{x = 12}
 \end{array}$$

**Exercise 1:** Solve each of the following equations using whatever way you wish.

1.  $5x + 12 = 3x + 2$

$$\begin{array}{r}
 5x + 12 = 3x + 2 \\
 -3x \quad -3x \\
 \hline
 2x + 12 = 2 \\
 -12 \quad -12 \\
 \hline
 2x = -10 \\
 \frac{2x}{2} = \frac{-10}{2} \\
 \boxed{x = -5}
 \end{array}$$

Verify the solution: Plug  $x = -5$  back in.

$$\begin{array}{rcl}
 5x + 12 & = & 3x + 2 \\
 5(-5) + 12 & = & 3(-5) + 2 \\
 -25 + 12 & = & -15 + 2 \\
 -13 & = & -13 \checkmark
 \end{array}$$

2.  $5m + 3 = -7 - 5m$

$$\begin{array}{r}
 5m + 3 = -7 - 5m \\
 5m \quad +5m \\
 \hline
 10m + 3 = -7 \\
 -3 \quad -3 \\
 \hline
 10m = -10 \\
 \frac{10m}{10} = \frac{-10}{10} \\
 \boxed{m = -1}
 \end{array}$$

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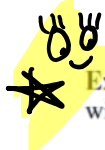
In some equations you will have to combine like terms on each side, before solving.

Example 2: Solve  $4k + 8 - 2k - 3 = 8 - 4k + 9$  by collecting like terms first.

$$\begin{aligned}
 4k - 2k + 8 - 3 &= -4k + 17 \\
 2k + 5 &= -4k + 17 \\
 +4k & \quad +4k \\
 \hline
 6k + 5 &= 17 \\
 -5 & \quad -5 \\
 \hline
 6k &= 12 \quad \rightarrow \boxed{k=2}
 \end{aligned}$$

Example 3: Solve the following equations. Note: If an equation has brackets, distribute first. (multiply)

$$\begin{aligned}
 2(4x-3) &= 3(2x+4) \\
 2(4x) + 2(-3) &= 3(2x) + 3(4) \\
 8x - 6 &= 6x + 12 \\
 -6x & \quad -6x \\
 \hline
 2x - 6 &= 12 \\
 +6 & \quad +6 \\
 \hline
 2x &= 18 \\
 \div 2 & \quad \div 2 \\
 \boxed{x=9}
 \end{aligned}$$



Ex. 11: Ben and Hines want to rent scooters while on a vacation. They come across two rental shops with the following rates:

Scooter-World	\$17 for the first hour, \$16 for each additional hour.
Vespa-Ville	\$35 for the first hour, \$12 for each additional hour

Ben decides to rent from Scooter-World and Hines rents from Vespa-Ville. How long would they have to ride for to pay the exact same rental amount?



↳ the 2 costs are equal.

Let  $h$  = # of hours extra

Scooter World: cost =  $17 + 16x$

Vespa-Ville: cost =  $35 + 12x$

$$17 + 16x = 35 + 12x$$

$$\begin{aligned}
 17 + 16x &= 35 \\
 -17 & \quad -17 \\
 \hline
 4x &= 18
 \end{aligned}$$

$$4x = 18 \quad \div 4 \quad \div 4 = \frac{9}{2}$$

$$\boxed{x = 4.5} \text{ hours}$$

Assignment: "What is the Title of This Picture?" & "How Can You Visit the Sun Without Burning Up (do #5!!)"

The cost is the same if they ride for 4.5 hours.

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