

Factoring

FOM 11

Practice Partial Factoring + Find Equation of Parabola

① Use Factoring to graph

$y = x^2 + 6x + 5$. Find

$\begin{array}{r} \boxed{1} \times \boxed{5} = 5 \\ \boxed{1} + \boxed{5} = 6 \\ \hline x \quad x \\ 1 \quad 5 \end{array}$

a) The factored form,

$(x + ?)(x + ?)$

b) the x-intercepts $x = -1$ & $x = -5$

because $(x+1)(x+5) = 0$
means $x+1=0$ OR $x+5=0$
 $x = -1$ OR $x = -5$

c) the axis of symmetry

$x = \frac{-1 + -5}{2} = \frac{-6}{2} = -3$ $x = -3$

d) the vertex

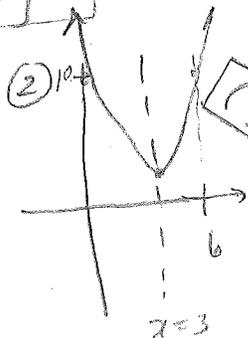
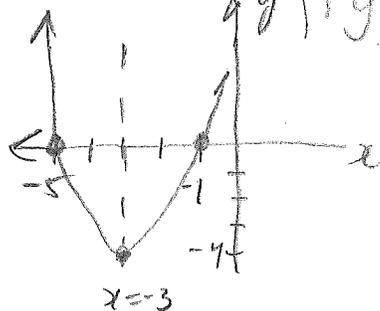
Plus in $x = -3$: $y = (-3)^2 + 6(-3) + 5$
 $y = 9 - 18 + 5 = -4$

e) the domain

$\{x \mid x \in \mathbb{R}\}$

f) the range

$\{y \mid y \geq -4\}$



② $y = x^2 - 6x + 10$

does not factor! Use partial factoring.

a) Rewrite the above but

with the 1st 2 terms

factored
 $y = x(x-6) + 10$
 $y = ?(x-?) + 10$

b) set the factored part

to 0. what $x(x-6) = 0$
so $x=0$ OR $x-6=0$
x-values do you get? $x=6$

c) what are the

$x = 0, x = 6$

corresponding points? $(0, 10)$
 $(6, 10)$

d) the axis of symmetry?

$x = \frac{0+6}{2} = \frac{6}{2} = 3$ $x = 3$

e) the vertex?

Plug in $x = 3 \Rightarrow y = 3^2 - 6(3) + 10$
 $y = 9 - 18 + 10$

f) the domain?

$\{x \mid x \in \mathbb{R}\}$

g) the range?

$\{y \mid y \geq 1\}$

③ Find the quadratic equation for this parabola.

Notice

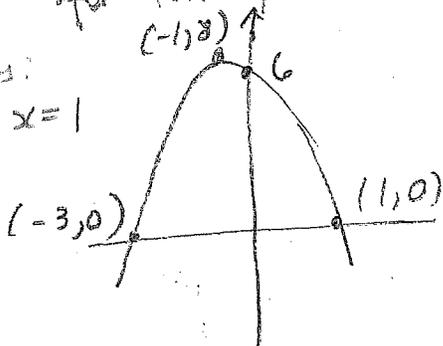
x-intercepts:

$x = -3$ & $x = 1$

y-int:

$(0, 6)$

use Δ as x \uparrow as y



Hint: $y = a(x-r)(x-s)$

• Plug in a point (x, y) & solve for a.

$y = a(x+3)(x-1)$

$6 = a(0+3)(0-1)$

$6 = a(-3)$

$\frac{6}{-3} = \frac{-2}{-3}$ so $y = -2(x+3)(x-1)$

opposite of the x-intercepts

↑
opp. of x-intercepts